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PII: S0957-4174(22)01808-5

DOI: <https://doi.org/10.1016/j.eswa.2022.118790>

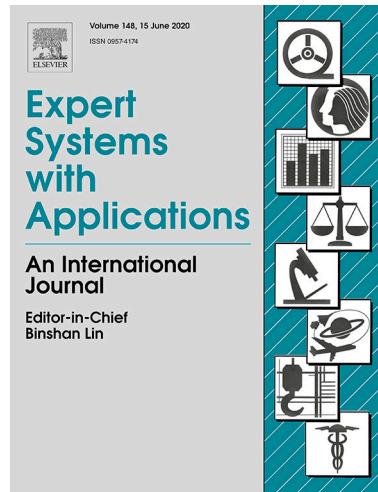
Reference: ESWA 118790

To appear in: *Expert Systems with Applications*

Received Date: 30 March 2022

Revised Date: 25 August 2022

Accepted Date: 4 September 2022



Please cite this article as: Zeng, J., Tang, J., Combining knowledge graph into metro passenger flow prediction: a split-attention relational graph convolutional network, *Expert Systems with Applications* (2022), doi: <https://doi.org/10.1016/j.eswa.2022.118790>

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# Combining knowledge graph into metro passenger flow prediction: a split-attention relational graph convolutional network

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1 **Abstract:**

2 With the rapid development of intelligent operation and management in metro systems, accurate  
 3 network-scale passenger flow prediction has become an essential component in real-time metro  
 4 management. Although numerous novel methods have been applied in this field, critical barriers  
 5 still exist in integrating travel behaviors and comprehensive spatiotemporal dependencies into  
 6 prediction. This study constructs the metro system as a knowledge graph and proposes a split-  
 7 attention relational graph convolutional network (SARGCN) to address these challenges. Breaking  
 8 the limitations of physical metro networks, we develop a metro topological graph construction  
 9 method based on the historical origin-destination (OD) matrix to involve travel behaviors. Then, we  
 10 design a metro knowledge graph construction method to incorporate land-use features. To adapt  
 11 prior knowledge of metro systems, we subsequently propose the SARGCN model for network-scale  
 12 metro passenger flow prediction. This model integrates the relational graph convolutional network  
 13 (R-GCN), split-attention mechanism, and long short-term memory (LSTM) to explore the  
 14 spatiotemporal correlations and dependence between passenger inflow and outflow. According to  
 15 the model validation conducted on the metro systems in Shenzhen and Hangzhou, China, the  
 16 SARGCN model outperforms the advanced baselines. Furthermore, quantitative experiments also  
 17 reveal the effectiveness of its component and the constructed metro knowledge graph.

18 **Keywords:** passenger flow prediction, urban metro system, knowledge graph, graph neural network,  
 19 deep learning

20 **1. Introduction**

21 Among all modes of urban public transportation, the metro system has attracted attention from  
 22 transportation planners and managers due to its advantages of high speed, large capacity, and  
 23 punctuality. Although these advantages help the metro system attract more passengers, the  
 24 imbalance between travel demands and services has become increasingly severe. Many metro  
 25 stations, especially the critical nodes in the metro network, always face the intense challenge of  
 26 congestion. These issues negatively affect on the travel experience of passengers and reduce the  
 27 attractiveness of metro systems.

28 In recent years, since many compelling scenarios of the internet of things (IoT) have been applied  
 29 in metro operations, transportation administration can quickly obtain real-time states of the metro  
 30 system. Based on real-time information from advanced data collection and processing technologies,  
 31 numerous emerging applications have been conducted. To relieve pressure in metro operations, the  
 32 administration not only needs to grasp the current conditions but also to forecast their future  
 33 variations in advance. Therefore, accurate passenger flow prediction in metro systems has become  
 34 an essential task in recent years.

35 According to the prediction horizons, metro passenger flow prediction can be classified into three  
 36 major categories (Ma et al., 2019): long-term, medium-term, and short-term prediction. Long-term  
 37 and medium-term passenger flow predictions are vital in metro planning and development. For these  
 38 purposes, researchers mainly employ the four-step travel demand forecasting model (Agrawal et al.,  
 39 2018; McNally, 2007) and geographically weighted regression (GWR) (Daniel et al., 2012) to  
 40 predict future (e.g., monthly, annual, etc.) demand. Generally, the abovementioned two prediction  
 41 tasks focus on metro policy and planning, but they cannot meet the needs of real-time applications.  
 42 Since real-time information is beneficial to avoiding congestion and balancing transportation  
 43 resources (Zhang et al., 2020b), the importance of short-term passenger flow prediction is

1 increasingly highlighted.

2 Previous studies on short-term passenger flow prediction can be further divided into station-level  
 3 and network-scale predictions. The former aims to forecast the future passenger flow of a specific  
 4 station. Since the temporal dependence of passenger flow is the basis of this task, the involved  
 5 prediction methods include statistical methods, machine learning methods, and recurrent neural  
 6 network (RNN) based deep learning methods. In the opposite, the latter focuses on predicting future  
 7 passenger flows of each station simultaneously. In addition to the temporal dependence, exploring  
 8 the spatial correlation is also essential to achieving accurate predictions. Therefore, several novel  
 9 deep learning models with powerful spatial correlation extraction capability, e.g., convolutional  
 10 neural network (CNN) and graph neural network (GNN), have widely attracted the attention of  
 11 researchers.

12 Since the abovementioned station-level prediction models rarely consider the spatial correlation  
 13 in the metro network, these models always suffer from limited prediction performance. Furthermore,  
 14 this category of prediction models needs to conduct training on each station separately, so the  
 15 training and storage costs approximately linearly increase with the metro network scale. Overall,  
 16 the station-level prediction methods are unsuitable for predicting future passenger flows of all the  
 17 stations in the metro network. Therefore, in recent years, researchers have preferred network-scale  
 18 prediction models. As there are typical topological structures in metro systems, GNNs are widely  
 19 applied in this field and have consistently achieved state-of-the-art performance.

20 Although numerous novel methods have been applied in this field, several critical issues are still  
 21 unaddressed:

22 (1) In GNN-based models, researchers must construct a reasonable graph in advance, which plays  
 23 a vital role in prediction performance. In numerous studies, the graphs are directly established  
 24 according to the physical adjacency relationship (i.e., the topology of the metro network) (Han et  
 25 al., 2019; Ye et al., 2020; Zhang et al., 2020b). However, these graph construction methods always  
 26 overlook metro travel behaviors. Thus, how to fuse travel behaviors and features into graph  
 27 construction principles still needs further exploration.

28 (2) Travel demands and behaviors are significantly associated with land-use characteristics (Jun  
 29 et al., 2015), but only a few studies (He et al., 2020; Lin et al., 2020) consider this vital factor in  
 30 metro passenger flow prediction. These studies attempt to address metro passenger flow prediction  
 31 using statistical methods or shallow machine learning methods, so there is a lack of exploration of  
 32 the spatiotemporal dependencies in network-scale passenger flow. GNNs are always regarded as  
 33 powerful tools in this field (Han et al., 2019; Liu et al., 2020; Ye et al., 2020; Zhang et al., 2020b),  
 34 but land-use features are rarely introduced into GNNs for metro passenger flow prediction. Thus,  
 35 effectively integrating the land-use features and GNN model to improve prediction accuracy is still  
 36 a challenge.

37 (3) Spatiotemporal correlations of passenger flow at different stations need further mining to  
 38 improve prediction performance. There are two passenger flows at each metro station: inflow (i.e.,  
 39 the number of passengers in the origin station) and outflow (i.e., the number of passengers in the  
 40 destination station). Since the outflow of each station consists of the inflow of the remaining stations  
 41 in the metro network, the inflow and outflow are correlated in the spatial and temporal dimensions.  
 42 However, few current studies explore this relationship in passenger flow prediction. Additionally,  
 43 passenger flows in different regions also follow specific travel patterns. For instance, commuting  
 44 will cause the metro passenger flow around industrial and residential regions to show the opposite

1 trend. These spatiotemporal regularities are also vital for metro passenger flow analysis and  
2 prediction.

3 To fill these gaps, we propose a deep learning framework for short-term metro passenger flow  
4 prediction, named split-attention relational graph convolutional network (SARGCN). To adapt  
5 metro travel behaviors and operation principles, we extract the historical OD matrix from the smart  
6 card data as the similarity measure and employ the complex network construction method  
7 (Cupertino et al., 2013) to establish a topological graph. Since land-use features significantly impact  
8 metro travel demands and behaviors, we introduce the point of interest (POI) data to transform the  
9 constructed topological graph into a metro knowledge graph. Then, a spatiotemporal learning  
10 framework, i.e., the SARGCN, is proposed for network-scale metro passenger flow learning and  
11 prediction based on the established knowledge graph. In summary, the major contributions of this  
12 study are concluded as follows:

13 (1) We develop a metro topological graph construction method based on the historical OD matrix  
14 and complex network construction algorithm. Compared with the physical metro network, this data-  
15 driven graph construction method is adaptive to metro travel patterns, so the spatial correlation on  
16 the graph is enhanced.

17 (2) Based on the land-use features around metro stations, a metro knowledge graph construction  
18 method is designed and applied to the constructed metro topological graph. In this way, each station  
19 is assigned a specific semantic type to provide essential prior knowledge for the deep learning  
20 model.

21 (3) We propose the SARGCN model for network-scale metro passenger flow prediction. In this  
22 model, the R-GCN, split-attention mechanism, and LSTM are effectively incorporated to learn the  
23 spatiotemporal correlations and dependencies between inflow and outflow on the constructed metro  
24 knowledge graph.

25 (4) Validated on the metro systems in Shenzhen and Hangzhou, China, the proposed SARGCN  
26 model expresses a superior performance than the advanced baselines in terms of accuracy and  
27 efficiency. Additionally, the ablation experiment results also demonstrate the effectiveness of each  
28 component.

29 The organization of this paper is summarized as follows. Section 2 discusses the existing studies  
30 in the field of short-term metro passenger flow prediction. We briefly describe the metro passenger  
31 flow and land-use data involved in this study in Section 3. Section 4 introduces the detailed  
32 methodology of the proposed metro knowledge construction method and SARGCN model. Section  
33 5 shows the experimental results and discussions. Finally, we conclude this study and summarize  
34 the research directions for future works in Section 6.

## 35 **2. Literature review**

### 36 **2.1 Station-level prediction methods**

37 Due to the limitation of computing capability, statistical methods won the favor of researchers in  
38 the early stage of metro passenger flow prediction. Statistical methods always regard the previous  
39 ridership of each station as sequence data and employ time-series analysis models to make  
40 predictions. Among all the time-series analysis models, the autoregressive integrated moving  
41 average (ARIMA) model (Chen et al., 2020; Wen et al., 2022) and its variants are the most famous  
42 methods in metro passenger flow prediction. Meanwhile, other statistical methods, such as the

1 Kalman filter (Sun et al., 2014) and generalized autoregressive conditional heteroskedasticity  
 2 (GRACH) (Ding et al., 2018), are also widely applied in this task. However, these statistical methods  
 3 always encounter limitations in exploring the nonlinear characteristics of traffic data (Zhao et al.,  
 4 2020a) and have high computational complexity (Zhang et al., 2019). Additionally, these methods  
 5 may encounter challenges when facing complex conditions and big data (Zhou et al., 2020).

6 To fill these gaps, numerous machine learning models have been developed for metro passenger  
 7 flow prediction, including artificial neural network (ANN) (Li et al., 2019; Li et al., 2017b; Wei &  
 8 Chen, 2012; Zhao et al., 2011), support vector machine (SVM) (Sun et al., 2015; Tang et al., 2019a),  
 9 decision trees (Ding et al., 2016; Zhao et al., 2020b), and Bayesian networks (Lin et al., 2017; Roos  
 10 et al., 2017). Although these machine learning methods can usually achieve higher prediction  
 11 accuracies than traditional statistical methods, their prediction performances are still unsatisfactory  
 12 for real-time applications of metro systems. Meanwhile, machine learning methods always face  
 13 significant challenges to capturing the temporal dynamics in passenger flow. Facing a dramatic  
 14 increase in the scale of metro data and metro management demands, researchers widely apply  
 15 deep learning methods in this field and have demonstrated their superiority to traditional methods.  
 16 Since metro passenger flow is highly temporally dependent, recurrent neural network (RNN) and  
 17 its famous variants, i.e., long short-term memory (LSTM) (Tang et al., 2019b) and gated recurrent  
 18 unit (GRU) (Zhang & Kabuka, 2018) are widely employed to mine its time-varying dynamics.  
 19 Meanwhile, to improve prediction performance under anomalous large passenger flow, (Zheng et  
 20 al., 2020) employed the complex network theory to collective behavior modeling, and then a hybrid  
 21 model was subsequently proposed to capture the time-varying characteristics of passenger flow.

## 22 **2.2 Network-scale prediction methods**

23 To solve the limitation of traditional station-level prediction methods, many researchers have paid  
 24 attention to network-scale passenger flow prediction models. Hao et al. (2019) proposed a sequence  
 25 to sequence (Seq2Seq) model based on LSTM and the attention mechanism for network-scale  
 26 passenger prediction. Additionally, this model further introduced external features (e.g., weather,  
 27 special events, etc.) into the prediction framework. Ma et al. (2019) transformed metro ridership  
 28 into grid-based data and then combined CNN with bidirectional LSTM to construct a parallel  
 29 architecture for prediction. Ning et al. (2018) designed a residual unit and introduced external factors  
 30 into metro passenger flow prediction. However, since metro stations are sparsely distributed in the  
 31 urban areas, Liu et al. (2019) demonstrated that metro networks are unsuitable for transforming into  
 32 grid-based data. Hence, they manually designed high-level features to represent the spatial  
 33 correlation to achieve accurate prediction.

34 To further promote passenger flow prediction accuracy, researchers also turned to GNN-based  
 35 methods to involve topological information in prediction models. Zhang et al. (2020b) integrated  
 36 the ResNet (He et al., 2016), GCN (Kipf & Welling, 2016), and attention-based LSTM to construct  
 37 the ResLSTM model for metro passenger flow prediction. Ye et al. (2020) proposed a Multi-  
 38 STGCnet model, which employed the LSTM and GCN to extract the temporal and spatial  
 39 dependencies of metro passenger flow, respectively. Relying on the physical metro network, Wang  
 40 et al. (2021) constructed metro hypergraphs to involve OD passenger flow and proposed a dynamic  
 41 spatiotemporal hypergraph neural network (DSTHGCN) for prediction. Ou et al. (2020) integrated  
 42 diffusion graph convolutional networks with a novel temporal convolutional model (i.e., TrellisNet  
 43 (Bai et al., 2019b)) to explore the spatiotemporal dependencies of metro passenger flow.

1     Actually, there is a typical *tunnel effect* from the perspective of metro operation regularities and  
 2     passenger travel behaviors. That is, passengers are more inclined to take the metro on long-distance  
 3     travel instead of going to the nearby stations. Therefore, it is challenging for physical metro  
 4     networks to capture this travel behavior. Liu et al. (2020) proposed a physical-virtual collaboration  
 5     graph network (PVCGN) model, which integrates a physical graph, a similarity graph, and a  
 6     correlation graph for metro ridership and online OD ridership prediction. However, the similarity  
 7     graph and correlation graph are based on the  $k$ -nearest neighbors (i.e., connecting each node to its  
 8      $k$  most similar nodes) and the  $\varepsilon$ -radius principles (i.e., connecting each node to nodes within  
 9     distance threshold  $\varepsilon$ ). Thus, the constructed network only focuses on the similarity at the node level  
 10    while ignoring the optimality at the network level. Meanwhile, land-use features are also a typical  
 11    factor to represent the travel behavior of metro passenger flow, but they are rarely considered in  
 12    network-scale passenger flow prediction. Overall, a brief summary of this study and current novel  
 13    models in this field is displayed in Table 1.

14    Table 1 Comparison of network-scale prediction models in metro passenger prediction

	Land-use features	Travel behavior	Correlation of in & out flow
ResLSTM	✗	✗	✓
DSTHGCRN	✗	✓	✗
PVCGN	✗	✓	✓
SARGCN	✓	✓	✓

15    3. Data description

16    3.1 Metro data

17    This study applies the smart card data collected in Shenzhen and Hangzhou, China, to validate  
 18    the proposed model. The smart card records include smart card ID, collection machine ID, state (i.e.,  
 19    enter or exit), collection time, metro line, and metro station. Passenger travel features, such as the  
 20    travel time matrix and OD matrix, can be extracted from this data source. We count the number of  
 21    passengers entering and leaving each station from the original smart card records, named inflow and  
 22    outflow. Furthermore, we also extract the historical OD matrix from the smart card records to  
 23    measure the spatial dependence between different metro stations.

24    The detailed descriptions of these two datasets are introduced as follows:

25    (1) **Shenzhen city.** The Shenzhen metro network includes 166 metro stations, and the collection  
 26    duration of smart card records ranges from May 1<sup>st</sup> to May 31<sup>st</sup> in 2019. According to the actual  
 27    operation time of the metro system, only the records between 6:00 am and 11:00 pm are used in this  
 28    study. For this dataset, we aggregate the inflow and outflow of each station every 10 minutes. Thus,  
 29    the inflow and outflow of each station can be regarded as a time-series with 102 records per day.

30    (2) **Hangzhou city.** This dataset is released by (Liu et al., 2020) via an accessible link<sup>1</sup>. In this  
 31    dataset, there are 80 metro stations in total. All the data is collected in January 2019, and the time  
 32    interval of passenger flow is set as 15 minutes.

<sup>1</sup><https://github.com/HCPLab-SYSU/PVCGN>

1 **3.2 Land-use data**

2 Lin et al. (2020) demonstrated that land-use features vitally affected metro passenger flows. POI  
 3 data refer to specific points with different functional attributions in urban areas and are widely used  
 4 in travel pattern analysis (Krause & Zhang, 2019). Therefore, we utilize the POI data to reflect the  
 5 land-use characteristics around each metro station for passenger flow analysis and prediction. The  
 6 POI data involved in this study are collected by the application programming interface (API) of  
 7 Baidu Map<sup>2</sup>. The original POI data have 19 categories and 140 subcategories. We merge similar  
 8 categories according to the definition of land-use attributes and finally obtain five categories. The  
 9 detailed descriptions of these five merged categories are displayed in Table 2.

10 Table 2 Classification and description of POI data

Category	Contents
residential area	residential area, dormitory, etc.
leisure and entertainment	restaurants, cinema, shopping center, etc.
education institution	colleges, high schools, kindergartens, etc.
corporate company	company, factory, etc.
transportation hub	airports, railway stations, bus stations, etc.

11 **4. Methodology**12 **4.1 Problem formulation**

13 Assume  $\mathbf{I}_t \in \mathbb{R}^{N \times M}$  and  $\mathbf{O}_t \in \mathbb{R}^{N \times M}$  denote the feature matrices of inflow and outflow at time  
 14 interval  $t$ , respectively, where  $N$  represents the number of stations and  $M$  denotes the number of  
 15 previous time steps. The metro passenger flow prediction task in this study can be summarized as  
 16 follows: given the previous passenger flow ( $\mathbf{I}_t$  and  $\mathbf{O}_t$ ) and a knowledge graph ( $\mathbb{G}$ ), aim to learn a  
 17 mapping function  $\mathbb{F}(\cdot)$  to predict inflow ( $\mathbf{i}_{t+p} \in \mathbb{R}^N$ ) and outflow ( $\mathbf{o}_{t+p} \in \mathbb{R}^N$ ) at the  $p$ -th step  
 18 afterward at each station.

$$(1) \quad (\mathbf{i}_{t+p}, \mathbf{o}_{t+p}) = \mathbb{F}(\mathbf{I}_t, \mathbf{O}_t; \mathbb{G})$$

19 **4.2 Metro knowledge graph construction**20 **4.2.1 Metro topological graph construction**

21 The *tunnel effect* mentioned above is an unignored characteristic in metro travel behavior.  
 22 According to the smart card data used in this study, the travel distance distribution in the Shenzhen  
 23 metro system is displayed in Figure 1. Here, we employ the Floyd-Warshall algorithm and metro  
 24 topological network to calculate the distance among metro stations. From this figure, an intuitive  
 25 finding is that the majority of passengers select the metro as middle-distance and long-distance  
 26 transportation, and few passengers take adjacent stations as their destinations. Specifically, the  
 27 average travel distance is 7.60 stations, and only 6% of passengers stop at adjacent stations. This  
 28 finding indicates that the passenger flow interactions between the adjacent metro stations are not

<sup>2</sup><https://lbsyun.baidu.com/index.php?title=webapi/guide/webservice-placeapi>

1 strong enough.

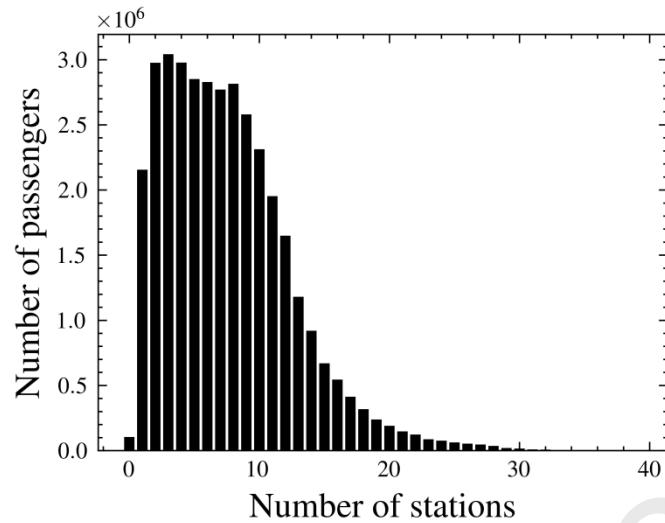
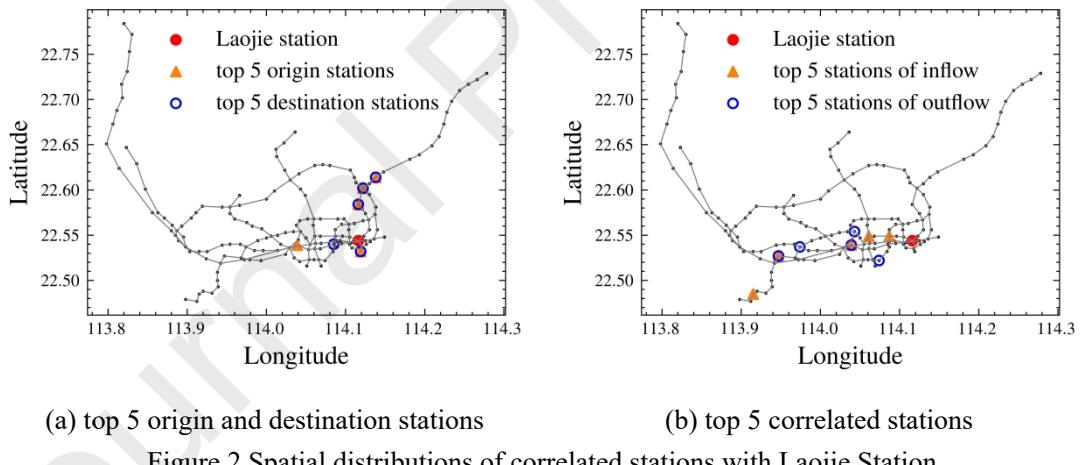


Figure 1 Travel distance distribution in the Shenzhen metro network

2 Furthermore, we illustrate the spatial distributions of the correlated stations for Laojie Station in  
 3 Figure 2. Laojie Station is an important node in the Shenzhen metro network, which is the transfer  
 4 station for Lines 1 and 3. Here, these four figures explore the positional relationship between Laojie  
 5 Station and its correlated stations from the traffic perspective (i.e., origin and destination stations)  
 6 and statistical perspective (i.e., Pearson correlation coefficient). Similarly, we can find that all the  
 7 correlated stations are far apart from Laojie Station, instead of the neighbor stations.



(a) top 5 origin and destination stations

(b) top 5 correlated stations

Figure 2 Spatial distributions of correlated stations with Laojie Station

8 Following these findings, since the topological network overlooks these travel patterns, it is  
 9 unsuitable for passenger flow prediction. Thus, it is essential to construct a reasonable graph that is  
 10 adaptive to the travel behaviors of the metro system. This study employs the OD relationship among  
 11 all the stations as the similarity measure for graph construction. Then, the complex network  
 12 construction algorithm proposed by (Cupertino et al., 2013) is applied to build a directed graph.  
 13 Unlike the simple  $k$ -nearest neighbors and the  $\varepsilon$ -radius approaches (Liu et al., 2020), this data-  
 14 driven construction method can connect correlated stations at the node level and consider optimality  
 15 at the network level. Cupertino et al. (2013) utilized a distance measure for graph construction, so  
 16 this method aimed to connect nodes with short distances. However, in this study, since we employ  
 17 the OD relationship as a similar measure, we prefer the OD passenger flow on the edges in the  
 18 constructed graph to be as large as possible. Thus, we replace the  $\min(\cdot)$  and  $\max(\cdot)$

1 operations in this method with the corresponding  $\max(\cdot)$  and  $\min(\cdot)$  operations, respectively.  
 2 Finally, we summarize this metro graph construction algorithm in Algorithm 1.

---

**Algorithm 1.** Metro topological graph construction method.

**Input:** number of nodes,  $N$ ; similarity matrix,  $\mathbf{W}_{OD} \in \mathbb{R}^{N \times N}$ ;  
 hyperparameters,  $K$  and  $\lambda$ ; node set  $\mathbf{V} = \{v_1, v_2, \dots, v_N\}$ .

**Output:** adjacency matrix,  $\mathbf{W}_g \in \mathbb{R}^{N \times N}$ .

**Process:**

```

1.  $\mathbf{W}_g \leftarrow \text{zeros}(N, N)$ 
2.  $\Omega \leftarrow \{\omega_1, \omega_2, \dots, \omega_N\}$  ( $\omega_i = \{v_i\}$ )
3.  $\mathbf{W}_\Omega \leftarrow \mathbf{W}_{OD}$ 
4. while  $\text{len}(\Omega) > 1$  do
5.    $[\omega_m, \omega_n] \leftarrow \text{argmax}(\mathbf{W}_\Omega)$ 
6.    $d_\varepsilon \leftarrow \lambda \cdot \min(d_m, d_n)$ 
7.    $[v_s, v_e] \leftarrow \text{select}(\omega_m, \omega_n, K)$ 
8.   for  $k=1, \dots, K$  do
9.     if  $\mathbf{W}[v_s^k, v_e^k] > d_\varepsilon$  do
10.       $\mathbf{W}_g[v_s^k, v_e^k] \leftarrow 1$ 
11.    end
12.   end
13.    $\omega_m \leftarrow \text{concat}(\omega_m, \omega_n)$  and delete  $\omega_n$ 
14.   update  $\mathbf{W}_\Omega$  among the current groups
15. end
16.  $\mathbf{W}_g[i, i] \leftarrow 1$ ,  $\forall i \in [1, N]$ 

```

---

3 In this algorithm, the **select**( $\cdot$ ) operation in Step 7 aims to select the most similar  $K$  node  
 4 pairs from  $\omega_m$  and  $\omega_n$ . Meanwhile,  $d_m$  and  $d_n$  represent the average similarity within node  
 5 groups  $\omega_m$  and  $\omega_n$ , respectively. In Step 13, **concat**( $\cdot$ ) denotes the concatenation operation,  
 6 which aims to join node groups  $\omega_m$  and  $\omega_n$  into a larger group. In Step 14,  $\mathbf{W}_\Omega[i, j]$  is updated  
 7 by the similarity of the most similar node pair between node groups  $\omega_i$  and  $\omega_j$ . Furthermore, since  
 8 the previous passenger flow of each station significantly affects its own future states, we apply a  
 9 self-loop connection (i.e., Step 16) to each node to retain its previous influence.

10 **4.2.2 Knowledge graph construction**

11 According to the definition in (Hogan et al., 2020), a knowledge graph is a network that consists  
 12 of entities with semantic types and relations between these entities. Since knowledge graphs can  
 13 truthfully and powerfully reflect the dependencies between entities in the real world, it has been  
 14 widely used in search engines, social networks, question answering, etc. In this study, we employ  
 15 the POI data around metro stations to represent their semantic types to obtain the metro knowledge  
 16 graph.

17 Determining the semantic types of nodes and relationships between them is the key step in  
 18 knowledge graph construction. In the previous study (Tang et al., 2020), POI data are generally  
 19 classified into several categories and employed to assign a label to each station, according to the  
 20 POI category with the maximum number around it. This method depends on the number of POI  
 21 categories around each metro station, but overlooks the differences in the total number of each  
 22 category. If there is a significant gap in the number of each category, it would be unfair to determine

1 the station type only based on the quantity. To obtain a more reasonable classification, we utilize  
 2 the distribution frequency of each category to determine the station type, which is summarized in  
 3 Equations 2 and 3. In these equations,  $c_i^j$  and  $p_i^j$  denote the number and distribution frequency of  
 4 POI category  $j$  around station  $i$ , respectively.  $\mathcal{R}_i$  represents the determined semantic type of  
 5 station  $i$ . In Equation 3, the type of each station is assigned as the POI category with the highest  
 6 distribution frequency.

$$p_i^j = \frac{c_i^j}{\sum_{k=1}^N c_k^j} \quad (2)$$

$$\mathcal{R}_i = \operatorname{argmax}_j p_i^j \quad (3)$$

7 Using the directed graph  $\mathcal{G}$  constructed above, we can establish a metro knowledge graph by  
 8 assigning the semantic types to corresponding stations. Therefore, the established knowledge graph  
 9 can be denoted as  $\mathbb{G} = (\mathcal{V}, \mathcal{E}, \mathcal{R})$ . Here,  $\mathcal{V}$ ,  $\mathcal{E}$ , and  $\mathcal{R}$  represent the node set, edge set, and node  
 10 types, respectively.

### 11 4.3 Framework of the SARGCN

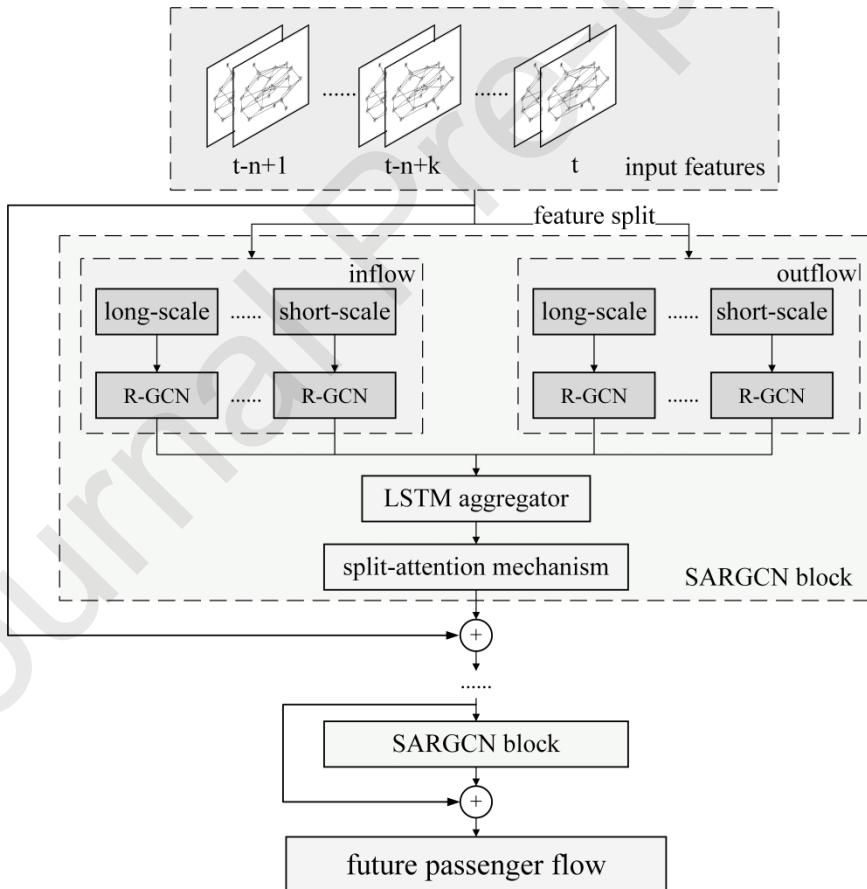


Figure 3 The framework of the proposed SARGCN model

12 Figure 3 illustrates the framework of the proposed prediction method. Based on the constructed  
 13 knowledge graph, we integrate the R-GCN, LSTM, and split-attention mechanism to construct the  
 14 SARGCN block. In each block, the R-GCN layer is applied to extract the spatial correlation on the  
 15 established knowledge graph. Meanwhile, we employ the split-attention mechanism and LSTM to

1 capture the temporal dynamics of passenger flow and explore the dependence between inflow and  
 2 outflow. The split-attention mechanism allows the input features to be divided into several groups.  
 3 Then, the unique characteristics of each group are extracted and aggregated to incorporate global  
 4 contextual information. After that, several SARGCN blocks are stacked together to improve the  
 5 capability of hidden feature extraction.

#### 6 4.4 Spatial correlation modeling

7 R-GCN (Schlichtkrull et al., 2018) is an effective variant of GCN, and it develops a powerful  
 8 capability to learn realistic knowledge bases. Thus, we adopt it to model the spatial dependence on  
 9 the constructed metro knowledge graph. Supposing the input feature of R-GCN is  $\mathbf{H} = \{\mathbf{h}_1, \mathbf{h}_2, \dots, \mathbf{h}_N\}$ , where  $\mathbf{h}_i$  denotes feature of node  $i$ , the calculation details of R-GCN are summarized in  
 10 Equation 4 and Figure 4.

$$\mathbf{h}'_i = \sigma \left( \sum_{r \in \mathcal{R}} \sum_{j \in \mathbb{N}_i^r} \frac{1}{c_{ir}} \mathbf{W}_r \mathbf{h}_j + \mathbf{W}_0 \mathbf{h}_i \right) \quad (4)$$

12

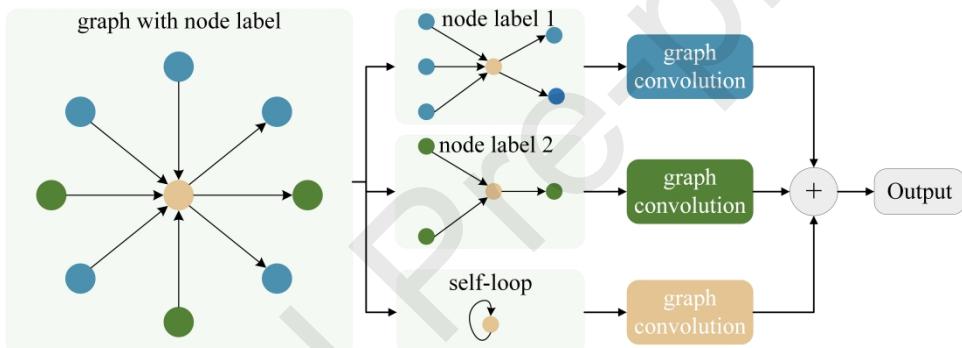


Figure 4 The calculation framework of R-GCN

13 Here,  $\mathcal{R}$  stands for the number of node types which is set as 5 according to Table 1, and  $\mathbb{N}_i^r$   
 14 denotes the neighbors of node  $i$  with type  $r$ .  $c_{ir}$  is a problem-specific normalization constant. To  
 15 highlight the importance of each node itself compared with its neighbors,  $\mathbf{W}_0$  is employed to  
 16 represent the particular connection type of the self-loops.

17 Moreover, a regularization, named basis decomposition, is applied in Equation 4 to reduce the  
 18 parameters by weight sharing. The regularization of  $\mathbf{W}_r$  is a linear combination and described in  
 19 Equation 5, where  $\mathbf{V}_b$  and  $\alpha_{rb}$  represent the learnable basis transformations and coefficients,  
 20 respectively.

$$\mathbf{W}_r = \sum_{b=1}^B \alpha_{rb} \mathbf{V}_b \quad (5)$$

#### 21 4.5 Temporal dependence modeling

22 In addition to the spatial correlation mentioned above, the metro passenger flow data still have  
 23 two dependencies: (i) temporal dynamics; (ii) the dependence between inflow and outflow. Both of  
 24 these dependencies are critical factors in improving prediction accuracy. Motivated by the  
 25 breakthrough of the ResNeSt model (Zhang et al., 2020a) in computer vision, we integrate its core  
 26 component, i.e., the split-attention mechanism, with R-GCN and LSTM model to model these two

1 vital dependencies. Specifically, the original split-attention mechanism employs the group  
 2 convolution operation (Krizhevsky et al., 2017; Xie et al., 2017) to extract the feature-map attention  
 3 and utilizes a weighted combination operation to mine global contextual information. Following  
 4 this opinion, using the split operation, we design a graph-based group convolution operation on the  
 5 previous passenger flow. Furthermore, since evident temporal dependence exists in passenger flow  
 6 data, we employ LSTM to address this time-series characteristic.

7 **4.5.1 Feature split operation**

8 Considering the dependence between inflow and outflow, we divide the previous passenger flow  
 9 into  $S$  split groups (e.g., inflow and outflow). In traffic prediction, researchers have demonstrated  
 10 that traffic data at different time steps show different influences on future states (Yang et al., 2019).  
 11 Therefore, in this study, we further classify each split group into  $C$  cardinal groups (e.g., long-  
 12 scale, middle-scale, and short-scale) according to the temporal dimension. Supposing the temporal  
 13 dimension of  $\mathbf{I}_t$  and  $\mathbf{O}_t$  is 6, the developed feature split operation under  $S = 2$  and  $C = 3$  is  
 14 illustrated in Figure 5. Since each subgroup uniquely affects future passenger flow, using different  
 15 models to capture the characteristics of each subgroup will help achieve accurate prediction results.

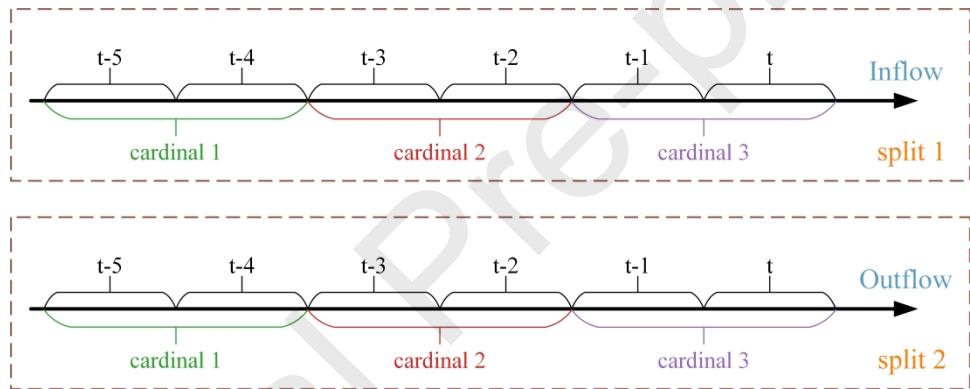


Figure 5 An example of the feature split operation under  $S = 2$ ,  $C = 3$

16 **4.5.2 Group graph convolution operation**

17 The group convolution plays a vital role in the split-attention mechanism. The principle of this  
 18 operation can be summarized as: output features can only receive information from input features  
 19 in the same group. Hence, we adopt this opinion and propose a group convolution operation. The  
 20 calculation process of the involved group R-GCN operation is summarized in Equations 6 and 7,  
 21 where  $\mathbf{h}_i^l$  denotes the input features of node  $i$  in group  $l$ , and  $\mathbf{h}_i^l$  represents the corresponding  
 22 output features. Meanwhile, the difference between the graph convolution operation and group  
 23 graph convolution is displayed in Figure 6.

$$\mathbf{h}_i^l = \sigma \left( \sum_{r \in \mathcal{R}_j \in \mathbb{N}_i^l} \sum_{r \in \mathcal{R}_j \in \mathbb{N}_i^l} \frac{1}{c_{ir}} \mathbf{w}_r \mathbf{h}_j^l + \mathbf{w}_0 \mathbf{h}_i^l \right) \quad (6)$$

$$\mathbf{h}_i' = \text{concat}(\mathbf{h}_i^{1'}, \mathbf{h}_i^{2'}, \dots, \mathbf{h}_i^{L'}) \quad (7)$$

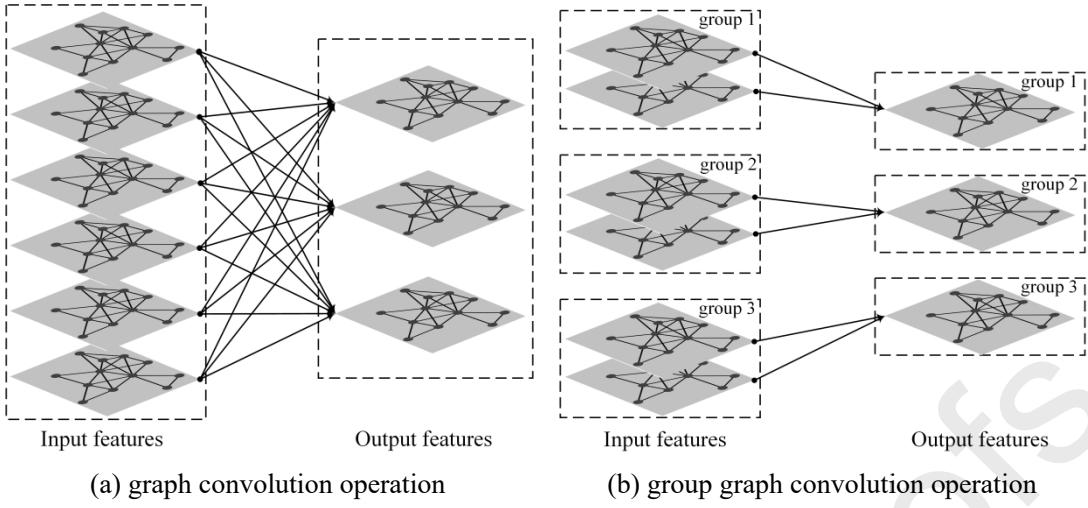


Figure 6 The structure of graph convolution operation and group graph convolution operation

#### 1 4.5.3 LSTM layer

2 As shown in Figure 5, we group the input features according to the temporal dimension. Thus,  
 3 temporal dependence exists among these groups. Many studies have demonstrated the strong ability  
 4 of LSTM to handle time-series data (Ma et al., 2015), so we employ it to model the temporal  
 5 dynamics among the output features of R-GCNs. The core composition of the LSTM unit includes  
 6 an input gate  $i_t$ , a forget gate  $f_t$ , an output gate  $o_t$ , and a memory cell  $c_t$ . Assuming  $x_t$  denotes  
 7 the input vector, the calculation process of the LSTM unit is described below.

$$i_t = \sigma(x_t \mathbf{W}_{xi} + \mathbf{h}_{t-1} \mathbf{W}_{hi} + \mathbf{b}_i) \quad (8)$$

$$f_t = \sigma(x_t \mathbf{W}_{xf} + \mathbf{h}_{t-1} \mathbf{W}_{hf} + \mathbf{b}_f) \quad (9)$$

$$o_t = \sigma(x_t \mathbf{W}_{xo} + \mathbf{h}_{t-1} \mathbf{W}_{ho} + \mathbf{b}_o) \quad (10)$$

$$\tilde{c}_t = \tanh(x_t \mathbf{W}_{xc} + \mathbf{h}_{t-1} \mathbf{W}_{hc} + \mathbf{b}_c) \quad (11)$$

$$c_t = f_t \odot c_{t-1} + i_t \odot \tilde{c}_t \quad (12)$$

$$h_t = o_t \odot \tanh(c_t) \quad (13)$$

8 Here,  $\mathbf{W}$  and  $\mathbf{b}$  represent the weight matrices and bias, respectively. In addition,  $\odot$  is the  
 9 elementwise product operation, and  $\sigma(\cdot)$  represents the sigmoid activation function.

#### 10 4.5.4 SARGCN block

11 Figure 3 indicates that the proposed SARGCN model consists of several stacked SARGCN  
 12 blocks. Relying on the description of R-GCN, feature split operation, and LSTM, we introduce the  
 13 SARGCN block in detail in this subsection (shown in Figure 7). Compared with the naive split-  
 14 attention mechanism in ResNeSt, we replace the convolution operation with R-GCN and utilize  
 15 LSTM to explore the temporal dynamics among groups.

16 As described in Section 4.1,  $\mathbf{I}_t$  and  $\mathbf{O}_t$  denote the input features of the SARGCN model. Taking  
 17 the first SARGCN block as an example, its output features  $\hat{\mathbf{V}}$  can be computed by the following  
 18 equations. Here, Equation 14 denotes the feature split process, and Equation 15 represents the R-  
 19 GCN operation. Equations 17-21 present the split-attention mechanism applied to the output  
 20 features of R-GCNs. Finally, a residual structure (described in Equation 22) is employed to enhance  
 21 the stability and improve the convergence speed in the training process.

22 In Equation 19,  $\xi^c(\cdot)$  represents two stacked dense layers with ReLU as the activation function.  
 23 And  $\mathbf{W}_F$  shown in Equation 22 is a learnable weight matrix that aims to transfer the dimension of

1 input features  $\mathbf{F}$  to be equal to that of  $\mathbf{V}$ .

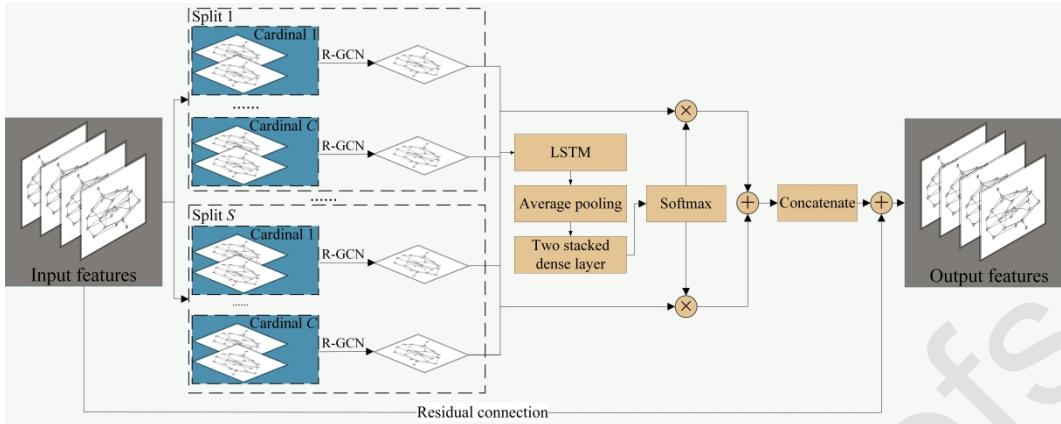


Figure 7 The detailed description of the SARGCN block

2 According to Equations 14-22, the proposed SARGCN block has a solid capability to explore the  
 3 spatiotemporal dependencies by integrating R-GCN, split-attention mechanism, and LSTM.  
 4 Specifically, R-GCN can capture the spatial correlation on the established knowledge graph and  
 5 explore the interactions between stations with different semantic types. The split-attention  
 6 mechanism can assign traffic significance to the deep learning model and effectively mine the  
 7 temporal dynamics and dependencies between inflow and outflow. Moreover, since passenger flow  
 8 data have typical time-series characteristics, LSTM is employed to enhance the capability of  
 9 SARGCN to handle this temporal correlation.

$$\mathbf{F} = \text{split}(\mathbf{I}_t, \mathbf{O}_t) = \{\mathbf{F}_1^1, \dots, \mathbf{F}_1^C; \dots; \mathbf{F}_S^1, \dots, \mathbf{F}_S^C\} \quad (14)$$

$$\mathbf{U}_s^c = \text{RGCN}_s^c(\mathbf{F}_s^c) \quad (15)$$

$$\tilde{\mathbf{U}} = \text{LSTM}(\mathbf{U}) = \{\tilde{\mathbf{U}}_1^1, \dots, \tilde{\mathbf{U}}_1^C; \dots; \tilde{\mathbf{U}}_S^1, \dots, \tilde{\mathbf{U}}_S^C\} \quad (16)$$

$$\tilde{\mathbf{U}}_s = \sum_{c=1}^C \tilde{\mathbf{U}}_s^c \quad (17)$$

$$\mathbf{S}_s = \text{average\_pooling}(\tilde{\mathbf{U}}_s) = \frac{1}{N} \sum_{n=1}^N \tilde{\mathbf{U}}_s(n) \quad (18)$$

$$a_s^c = \frac{\exp(\xi^c(\mathbf{S}_s))}{\sum_{j=1}^C \exp(\xi^j(\mathbf{S}_s))} \quad (19)$$

$$\mathbf{V}_s = \sum_{c=1}^C (a_s^c \cdot \tilde{\mathbf{U}}_s^c) \quad (20)$$

$$\mathbf{V} = \text{concat}(\mathbf{V}_1, \mathbf{V}_2, \dots, \mathbf{V}_S) \quad (21)$$

$$\hat{\mathbf{V}} = \mathbf{W}_V \mathbf{V} + \mathbf{W}_F \mathbf{F} \quad (22)$$

10 The proposed SARGCN model is a modular design by stacking SARGCN blocks. This modular  
 11 design idea makes the network structure relatively compact and convenient for building complex  
 12 and deep models. In this way, the model structure can be modified easily by changing the number  
 13 of groups (including split groups and cardinal groups) and the output dimension of R-GCN.  
 14 Compared with the naive R-GCN model, the split-attention mechanism can also help SARGCN  
 15 reduce model parameters and construct lightweight models.

## 16 5. Experiment

1    **5.1 Evaluation metrics**

2    In this study, three metrics are employed to evaluate prediction performance, including the root  
 3    mean square error (RMSE), mean absolute error (MAE), and mean absolute percentage error  
 4    (MAPE). The definitions of these three metrics are introduced in the following equations. Here,  $N$   
 5    denotes the number of metro stations, and  $n$  presents the number of testing samples. Meanwhile,  
 6     $y$  can represent both the ground-truth inflow and outflow, and  $\hat{y}$  denotes the corresponding  
 7    predicted values.

$$\text{RMSE} = \sqrt{\frac{1}{nN} \sum_{i=1}^N \sum_{j=1}^n (y_j^i - \hat{y}_j^i)^2} \quad (23)$$

$$\text{MAE} = \frac{1}{nN} \sum_{i=1}^N \sum_{j=1}^n |y_j^i - \hat{y}_j^i| \quad (24)$$

$$\text{MAPE} = \frac{1}{nN} \sum_{i=1}^N \sum_{j=1}^n \left| \frac{y_j^i - \hat{y}_j^i}{y_j^i} \right| \times 100\% \quad (25)$$

8    However, many studies have demonstrated that MAPE always faces significant challenges when  
 9    encountering zero or close-to-zeros ground truth (Kim & Kim, 2016). When the metro system begins  
 10   to operate in the early morning, no passengers exit at many stations, thus leading to zero data in  
 11   outflows. Therefore, we employ MAPE@10 (Zhang et al., 2019) to address this problem.  
 12   Specifically, we calculate MAPE on metro stations with the top 10% largest passenger flow.

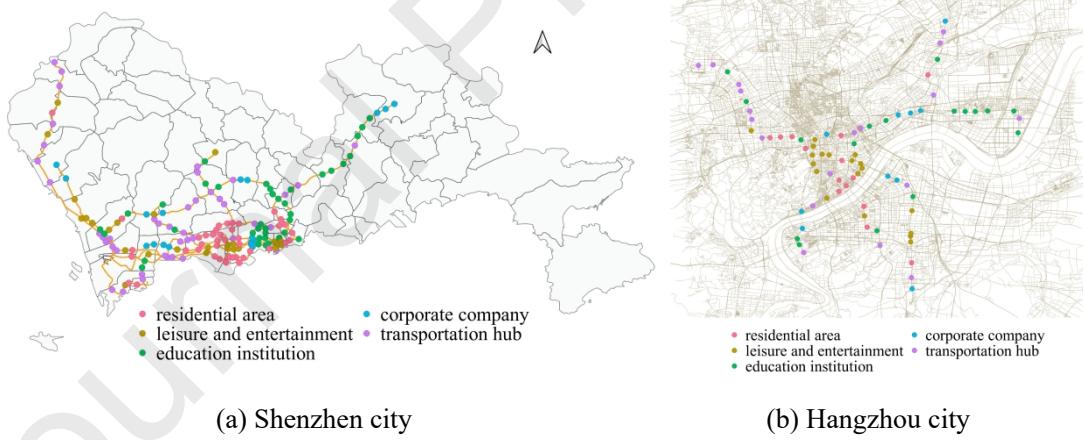


Figure 8 The spatial distribution of metro stations with different semantic types

13    **5.2 Experimental setting**

14    **5.2.1 Network construction method**

15    By using the construction method described in Section 4.2, we can transfer the employed  
 16   Shenzhen and Hangzhou metro systems into knowledge graphs, which are shown in Figure 8.  
 17   According to Algorithm 1, the network construction method has two critical parameters, named  $K$   
 18   and  $\lambda$ , which significantly impact network density. In this study, we set the value of  $\lambda$  as 0.1 and  
 19   assign the value of  $K$  to these two datasets as 7 and 13, respectively. Finally, the Shenzhen dataset  
 20   contains 166 nodes and 832 edges (including 166 self-loop edges). And in the Hangzhou dataset,

1 we obtain 80 nodes and 715 edges (including 80 self-loop edges).

2 **5.2.2 SARGCN model**

3 The implementation details of the proposed SARGCN model on the Shenzhen and Hangzhou  
4 metro systems are described as follows.

5 (1) **Shenzhen metro system.** As mentioned in Section 3.1, we aggregate both inflow and outflow  
6 into 10 minutes and finally obtain 3,162 records for each station. These passenger flow records are  
7 divided into a training set, a validation set, and a testing set according to a splitting rate of 70%:  
8 10%: 20%. We employ the previous 12 time-steps inflow and outflow to predict network-scale  
9 ridership at the next 1-step, 4-step, 7-step, and 10-step, respectively. Two stacked SARGCN blocks  
10 are utilized to compose the SARGCN model. The hidden dimension of the proposed SARGCN  
11 model is set to be the same as the number of stations, i.e.,  $N = 166$ . Considering the actual traffic  
12 significance, we set the number of groups in SARGCN as  $S = 2$  and  $C = 3$ . That is, we first divide  
13 passenger flow into two split groups (i.e., inflow and outflow), and each split group is further divided  
14 into three cardinal groups (i.e., short-scale flow, middle-scale flow, and long-scale flow).  
15 Meanwhile, we apply a grid search strategy on  $\{16, 32, 48, 64, 96\}$  to search for the optimal values of  
16 the hidden dimension of  $\xi$ . Finally, the prediction accuracy reaches the peak at 48, so we employ it  
17 as the optimal hyperparameter.

18 (2) **Hangzhou metro system.** Since this dataset is obtained from the open-source data (Liu et al.,  
19 2020), we follow all the settings of the original dataset. That is, we utilize the inflow and outflow  
20 of the previous 4 intervals to simultaneously predict the next 4 steps. Furthermore, a two-layer  
21 SARGCN model is employed to conduct passenger flow prediction in the Hangzhou metro network,  
22 and the hidden dimension is set as 224. After the grid search strategy, the hidden unit number of  $\xi$   
23 is set as 96. Since the horizontal of historical passenger flows is 4, we set the number of groups as  
24  $S = 2$  and  $C = 2$ .

25 Before inputting to the deep learning model, we first normalize these two datasets. The batch size  
26 of the mini-batch training strategy is set to 40 for Shenzhen and 32 (the same as in (Liu et al., 2020))  
27 for Hangzhou, and the Adam optimizer (Kingma & Ba, 2014) with a learning rate of 0.001 is applied  
28 for model training. All the parameters are initialized by Xavier initialization (Glorot & Bengio,  
29 2010). The number of training epochs is set to 300, and an early-stop strategy is adopted on the  
30 validation set to avoid overfitting.

31 **5.3 Performance comparison**

32 **5.3.1 Shenzhen metro system**

33 This subsection first introduces and employs 11 widely-used traffic state prediction models to be  
34 compared with the proposed SARGCN model on the Shenzhen metro system, including traditional  
35 statistical models, machine learning models, shallow deep learning models, and novel graph neural  
36 networks. The brief descriptions of the selected baselines are summarized below.

37 (1) **HA.** The historical average (HA) method utilizes the average passenger flows of each period  
38 to represent its future values. For instance, the future passenger flow at 7:00 am-7:10 am on the  
39 testing set is calculated by the average passenger flows during 7:00 am-7:10 am on the training set.  
40 We utilize the prediction performance of 1-step to denote that of multistep.

41 (2) **MLP.** The multilayer perceptron (MLP) is a basic machine learning model, and neither

1 temporal correlation nor spatial dependence is involved in this method. For each metro station, we  
 2 employ a 3-layer MLP, including an input layer, a hidden layer with ReLU as the activation function,  
 3 and an output layer to predict short-term passenger flow.

4 (3) **LSTM** (Ma et al., 2015). Long short-term memory (LSTM) can effectively capture the  
 5 temporal dynamics of metro passenger flow, but the spatial dependence is also overlooked.

6 (4) **GRU**. Gated recurrent unit (GRU) is a variant of LSTM. Similarly, only the temporal  
 7 correlation is used in this model.

8 (5) **GCN**. Considering the prediction performance, instead of the original GCN framework  
 9 proposed in (Kipf & Welling, 2016), we employ the R-GCN model without node types and edge  
 10 relationships (i.e., without a knowledge graph) as GCN to forecast short-term passenger flows.

11 (6) **GAT** (Velicković et al., 2017). The graph attention network (GAT) can explore spatial  
 12 dependence by the self-attention and multi-head attention mechanisms, and it has advantages in  
 13 directed graphs and inductive learning tasks. However, only spatial dependence is involved in the  
 14 naive GAT model.

15 (7) **STGCN** (Yu et al., 2018). In this model, the gated CNN is employed to capture the temporal  
 16 dynamics and combined with GCN to formulate the spatiotemporal graph convolutional network  
 17 (STGCN).

18 (8) **Graph-WaveNet** (Wu et al., 2019). In Graph-WaveNet, a novel adaptive correlation matrix  
 19 and stacked temporal convolutional layers are employed to handle spatial dependence and temporal  
 20 dynamics, respectively.

21 (9) **T-GCN** (Zhao et al., 2020a). This method utilizes GRU to capture the time-varying  
 22 characteristics of traffic data and applies GCN to explore the spatial correlation.

23 (10) **TGC-LSTM** (Cui et al., 2020). In this method, a traffic graph convolution operation based  
 24 on GCN is proposed and stacked with LSTM.

25 (11) **PVCGN** (Liu et al., 2020). This model constructs three topological graphs (including a  
 26 physical graph, a similarity graph, and a correlation graph) to explore the comprehensive spatial  
 27 correlations in the metro system. Then, a physical-virtual collaboration graph network (PVCGN) is  
 28 proposed to predict network-scale passenger flow.

29 All the experiments are conducted on a Windows 10 workstation (CPU: Intel Core (TM) i9-  
 30 9900K @ 3.6GHz, RAM: 32GB random-access memory, GPU: NVIDIA GTX 2080Ti with 11GB  
 31 memory) with Python 3.6.10. We implement the proposed SARGCN model with an open-source  
 32 graph learning framework, i.e., deep graph library (DGL) (Wang et al., 2019), and utilize MXNet  
 33 (Chen et al., 2015) as the backend.

34 Table 3 to Table 5 show the quantitative comparisons between SARGCN and baselines in the  
 35 Shenzhen metro system. The prediction performances shown in Table 3 consist of the whole  
 36 ridership, so we also separate the prediction metrics of inflow and outflow into Table 4 and Table  
 37 5, respectively. Here, the performances shown in Table 4 and Table 5 correspond to the metrics in  
 38 Table 3. Furthermore, we illustrate the ground-truth passenger flow and the predicted values of three  
 39 typical stations in Figure 9.

Table 3 Quantitative comparison of the whole ridership in Shenzhen metro system

	1-step			4-step			7-step			10-step		
	RMSE	MAE	MAPE@10									
HA	47.32	22.62	30.07%	47.32	22.62	30.07%	47.32	22.62	30.07%	47.32	22.62	30.07%
MLP	23.52	14.03	16.70%	34.20	19.30	25.74%	47.48	25.19	33.41%	59.87	30.61	38.78%
LSTM	23.73	13.82	18.11%	31.22	17.16	25.98%	40.80	20.78	35.07%	48.47	23.76	36.73%
GRU	23.93	14.07	19.24%	33.84	18.19	32.37%	45.45	22.46	47.16%	50.09	24.98	39.98%
GCN	23.35	13.80	15.57%	30.49	17.63	18.10%	42.63	24.36	26.37%	50.22	26.99	25.66%
GAT	20.24	12.41	21.38%	26.27	15.52	26.51%	33.03	18.85	31.62%	39.81	21.99	36.44%
STGCN	25.25	14.21	15.29%	34.98	18.80	19.51%	50.73	24.97	28.68%	67.79	32.07	41.65%
Graph-WaveNet	20.63	12.11	14.16%	24.47	13.29	15.42%	30.46	14.64	17.13%	32.09	15.49	18.84%
T-GCN	23.41	14.09	16.05%	28.11	16.32	19.40%	30.28	17.24	20.10%	32.18	18.75	23.16%
TGC-LSTM	22.59	14.22	18.56%	24.55	15.00	19.47%	28.33	16.32	23.08%	29.86	16.39	20.80%
PVCGN	22.63	12.76	14.27%	23.77	13.39	15.37%	24.46	13.64	16.39%	25.36	<b>13.99</b>	17.39%
SARGCN	<b>18.14</b>	<b>11.24</b>	<b>13.49%</b>	<b>20.85</b>	<b>12.52</b>	<b>15.10%</b>	<b>23.35</b>	<b>13.34</b>	<b>15.46%</b>	<b>24.51</b>	14.22	<b>17.34%</b>

Table 4 Quantitative comparison of inflow in Shenzhen metro system

	1-step			4-step			7-step			10-step		
	RMSE	MAE	MAPE@10									
HA	46.32	22.77	29.86%	46.32	22.77	29.86%	46.32	22.77	29.86%	46.32	22.77	29.86%
MLP	21.50	13.17	16.65%	34.47	19.56	28.54%	48.26	25.74	35.12%	60.17	30.99	39.72%
LSTM	21.36	12.82	18.73%	30.59	16.75	28.43%	40.77	20.61	33.83%	48.64	23.65	35.04%
GRU	21.48	13.01	19.77%	32.85	17.69	33.48%	44.51	22.10	43.77%	49.71	24.72	36.68%
GCN	21.37	12.79	15.05%	31.25	17.52	18.82%	44.37	24.69	27.73%	52.74	27.52	27.18%
GAT	18.55	11.49	14.03%	26.47	15.22	18.06%	34.77	19.28	20.65%	41.90	22.47	23.55%
STGCN	21.39	12.90	14.74%	33.35	17.64	19.01%	49.62	24.06	30.32%	69.17	31.94	45.74%
Graph-WaveNet	18.65	10.98	13.60%	22.99	12.48	<b>14.90%</b>	27.70	13.87	17.16%	28.76	14.77	19.36%
T-GCN	19.97	12.63	16.05%	26.70	15.58	19.40%	27.52	15.92	20.10%	31.44	18.29	23.16%
TGC-LSTM	21.52	13.79	18.98%	24.24	14.57	20.62%	28.71	15.91	23.94%	29.64	15.79	21.31%
PVCGN	20.99	11.74	13.75%	23.72	12.86	15.31%	24.82	13.21	16.39%	26.02	<b>13.60</b>	<b>17.14%</b>
SARGCN	<b>16.46</b>	<b>10.40</b>	<b>13.27%</b>	<b>20.58</b>	<b>12.17</b>	15.98%	<b>23.49</b>	<b>12.79</b>	<b>15.15%</b>	<b>24.35</b>	13.84	17.33%

These tables show that in terms of prediction accuracy on both the 1-step and multistep, SARGCN always expresses superior performances to the baselines. For instance, compared with the most accurate baseline in Table 3, SARGCN improves the RMSE by 10.38%, 12.28%, 4.54%, and 3.35% on these four steps, respectively. These results demonstrate that the proposed SARGCN model has a powerful capability to explore the spatiotemporal dependencies on the metro system. A comparison of the prediction results and ground truth (shown in Figure 9) shows that the time-varying patterns of passenger flow vary from station to station. And the proposed SARGCN model is effective in capturing these temporal dynamics in different time-varying patterns. Furthermore, compared with the baselines without spatial correlations (i.e., HA, MLP, LSTM, and GRU), almost all the GNN-based models perform higher accuracies in the 1-step prediction task and stabilities in multistep prediction tasks. This phenomenon further proves the importance of spatial correlations in metro passenger flow prediction. In summary, these comparisons can indicate the superior

Table 5 Quantitative comparison of outflow in Shenzhen metro system

	1-step			4-step			7-step			10-step		
	RMSE	MAE	MAPE@10									
HA	48.30	22.48	30.29%	48.30	22.48	30.29%	48.30	22.48	30.29%	48.30	22.48	30.29%
MLP	25.35	14.88	16.75%	33.92	19.05	22.88%	46.69	24.64	31.66%	59.56	30.23	37.82%
LSTM	25.87	14.82	17.48%	31.82	17.56	23.47%	40.83	20.94	36.34%	48.31	23.87	38.45%
GRU	26.13	15.11	18.68%	34.79	18.67	31.23%	46.37	22.82	50.63%	50.47	25.23	43.37%
GCN	25.17	14.81	16.10%	29.72	17.75	17.36%	40.83	24.03	24.98%	47.58	26.45	24.10%
GAT	21.79	13.31	15.01%	26.07	15.82	16.82%	31.21	18.42	19.16%	37.62	21.51	20.26%
STGCN	26.78	15.51	15.86%	36.53	19.94	20.03%	51.81	25.88	27.00%	66.38	32.19	37.47%
Graph-WaveNet	22.42	13.23	14.74%	25.84	14.09	15.96%	32.96	15.39	17.11%	35.08	16.21	18.31%
T-GCN	26.38	15.53	16.32%	29.43	17.05	17.96%	32.79	18.55	20.37%	32.90	19.21	20.76%
TGC-LSTM	23.61	14.65	18.13%	24.85	15.43	18.29%	27.95	16.73	22.21%	30.08	16.99	20.28%
PVCGN	24.15	13.77	14.81%	23.83	13.92	15.44%	24.03	14.06	16.38%	24.69	14.37	17.65%
SARGCN	<b>19.66</b>	<b>12.07</b>	<b>13.72%</b>	<b>21.10</b>	<b>12.88</b>	<b>14.19%</b>	<b>23.22</b>	<b>13.89</b>	<b>15.78%</b>	<b>24.67</b>	<b>14.59</b>	<b>17.34%</b>

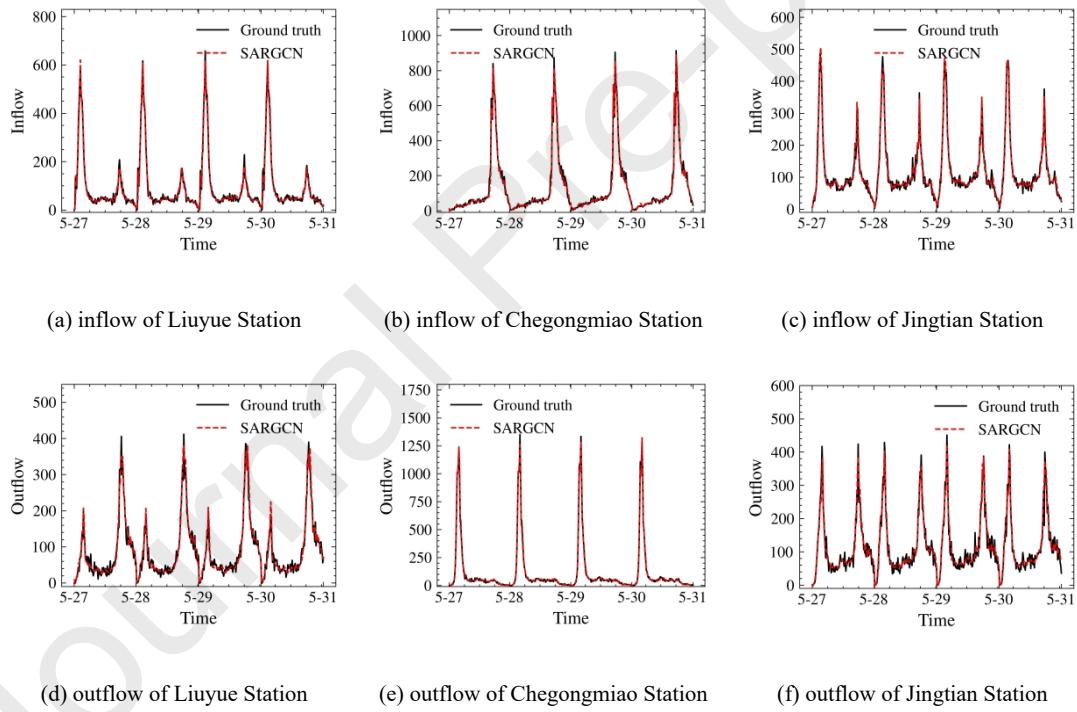


Figure 9 Comparison of prediction results and ground truth based on SARGCN model

1 performance of SARGCN on the Shenzhen metro dataset.

### 2 5.3.2 Hangzhou metro system

3 To evaluate the prediction performance of SARGCN model on the Hangzhou metro system, we  
4 directly introduce the experimental results in the previous study (Liu et al., 2020). The prediction  
5 performance in the Hangzhou metro system is summarized in Table 6. In the baselines, there are  
6 three traditional time series models, three general deep learning models, and six recently-proposed  
7 graph networks (i.e., ASTGCN (Guo et al., 2019), STG2Seq (Bai et al., 2019a), DCRNN (Li et al.,

1 2017a), GCRNN, Graph-WaveNet (Wu et al., 2019), PVCGN (Liu et al., 2020)). From this table,  
 2 we can find that the proposed SARGCN model can achieve the lowest RMSE and MAE at 15-min  
 3 among all the state-of-the-art methods. Although the MAE of PVCGN is lower than SARGCN with  
 4 the prediction horizontal increases, our SARGCN model always shows superior performance on  
 5 RMSE. Meanwhile, compared with the MAE of SARGCN, PVCGN reduces 0.55% (30-min),  
 6 0.86% (45-min), and 1.42% (60-min). However, compared with SARGCN, PVCGN increases the  
 7 RMSE by 3.99%, 3.91%, and 2.45% for 30-min, 45-min, and 60-min, respectively. According to  
 8 these experimental results, the improvement of SARGCN in RMSE is higher than the decrease in  
 9 MAE. Hence, these comparisons indicate that the proposed SARGCN model can achieve higher  
 10 prediction accuracy. However, since our SARGCN model lacks the Seq2Seq structure (Sutskever  
 11 et al., 2014), its prediction performance will decrease to a certain extent in long-scale prediction.  
 12

Table 6 Quantitative comparison of the whole ridership in Hangzhou metro system

	15 min			30 min			45 min			60 min		
	RMSE	MAE	MAPE	RMSE	MAE	MAPE	RMSE	MAE	MAPE	RMSE	MAE	MAPE
HA	64.19	36.37	19.14%	64.10	36.37	19.31%	63.92	36.23	19.57%	63.72	35.99	20.01%
RF	53.52	32.19	18.34%	64.54	38.00	21.46%	80.06	45.78	26.51%	94.29	52.95	37.12%
GBDT	51.50	30.88	17.60%	61.94	36.48	20.49%	76.70	44.12	25.75%	91.21	51.10	38.10%
MLP	46.55	26.57	16.26%	47.96	27.44	17.10%	50.66	28.79	19.01%	54.62	30.52	22.56%
LSTM	45.30	25.76	14.91%	45.52	26.01	15.10%	46.30	26.38	15.40%	47.53	26.76	16.34%
GRU	45.10	25.69	15.13%	45.26	25.93	15.35%	46.13	26.36	15.79%	47.69	26.98	17.20%
ASTGCN	46.19	27.34	15.05%	46.16	27.74	15.56%	46.79	28.20	16.48%	49.70	28.85	17.75%
STG2Seq	39.52	23.80	17.09%	40.72	24.72	19.51%	43.36	25.98	23.59%	46.05	26.50	27.93%
DCRNN	40.39	23.76	14.00%	42.57	25.22	14.99%	46.26	26.97	16.19%	49.35	28.47	18.16%
GCRNN	40.24	23.84	14.08%	41.95	25.14	14.86%	45.53	26.82	16.05%	50.28	28.75	17.89%
Graph-WaveNet	40.78	24.07	14.27%	42.80	25.48	15.23%	45.84	27.15	17.34%	49.89	29.14	19.37%
PVCGN	37.76	22.68	13.70%	39.34	23.33	13.81%	40.95	24.22	14.45%	42.61	24.93	15.49%
SARGCN	<b>36.22</b>	<b>22.48</b>	13.94%	<b>37.83</b>	23.46	14.99%	<b>39.41</b>	24.43	16.25%	<b>41.59</b>	25.29	17.60%

13 In addition to the prediction performance, we further compare the computational costs between  
 14 SARGCN and PVCGN on the Hangzhou dataset in Table 7. These comparisons are conducted on  
 15 the same workstation and batch size to ensure fairness. This table indicates that SARGCN can  
 16 reduce computational costs significantly. In particular, the number of parameters in SARGCN is  
 17 only 3.51% of those in PVCGN. This phenomenon demonstrates that the proposed SARGCN model  
 18 is much lighter than the state-of-the-art baseline. Furthermore, concerning the computational  
 19 efficiency, SARGCN is just 49.1% of PVCGN in the average training time of each epoch. Hence,  
 20 we can conclude that SARGCN can reduce training costs in terms of both the number of parameters  
 21 and training efficiency. Therefore, it is more friendly and suitable for real-world applications in  
 22 metro management.  
 23

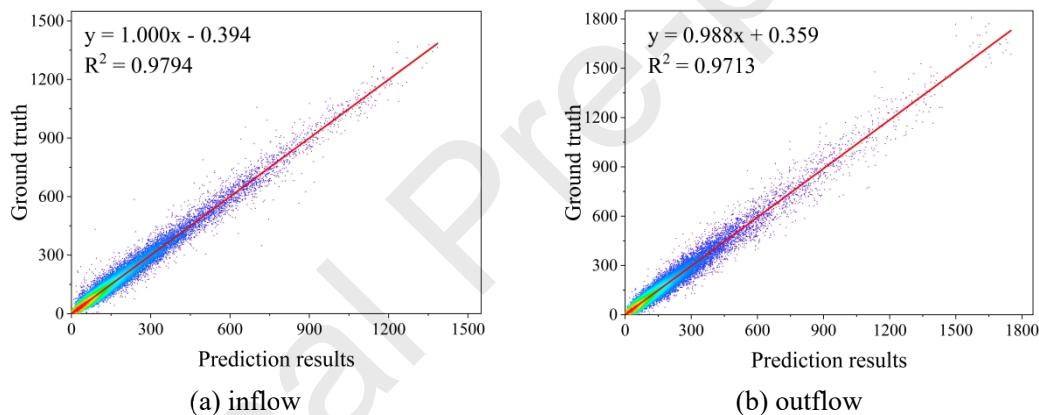
Table 7 Computational efficiency comparisons on the Hangzhou metro dataset

	PVCGN	SARGCN
Parameter amount	$3.76 \times 10^7$	$1.32 \times 10^6$
GPU occupation	7655 MiB	4859 MiB
Average training time	22.88 s/epoch	11.23 s/epoch

### 1 5.4 Error distribution analysis

2 The evaluation metrics shown in the above tables measure the prediction performance in terms  
 3 of average errors. To further validate the prediction accuracy, it is also essential to explore the error  
 4 distributions of each data point and station. Figure 10 expresses the actual distribution of ground  
 5 truth and prediction results of both inflow and outflow. As shown in these figures, the slopes of the  
 6 fitted lines are close to 1, thus indicating that the predicted values can effectively match the ground  
 7 truth. Although there are still errors, these data points are closely fitted and evenly distributed on  
 8 both sides of the fitted line. Meanwhile, the heatmaps show that the metro passenger flow is  
 9 concentrated at a lower level, and the quantity of data points decreases significantly with increasing  
 10 passenger flow. Overall, regardless of whether the passenger flow is large or small, SARGCN can  
 11 achieve reliable and accurate predictions.

12 In addition, we further explore the error distributions among all the metro stations. Different travel  
 13 patterns of each station may lead to different prediction performances. Thus, we employ RMSE and  
 14 MAE of each station to illustrate boxplots in Figure 11(a) and Figure 11(b), respectively. These two  
 15 figures indicate that there are fewer abnormal data in SARGCN, and its error indicators of boxplot  
 16 are generally lower than other models. This phenomenon reveals that SARGCN can always perform  
 17 more accurately on each metro station and reduce outliers.



18 Figure 10 Scatters and fitting of prediction results and ground truth of SARGCN

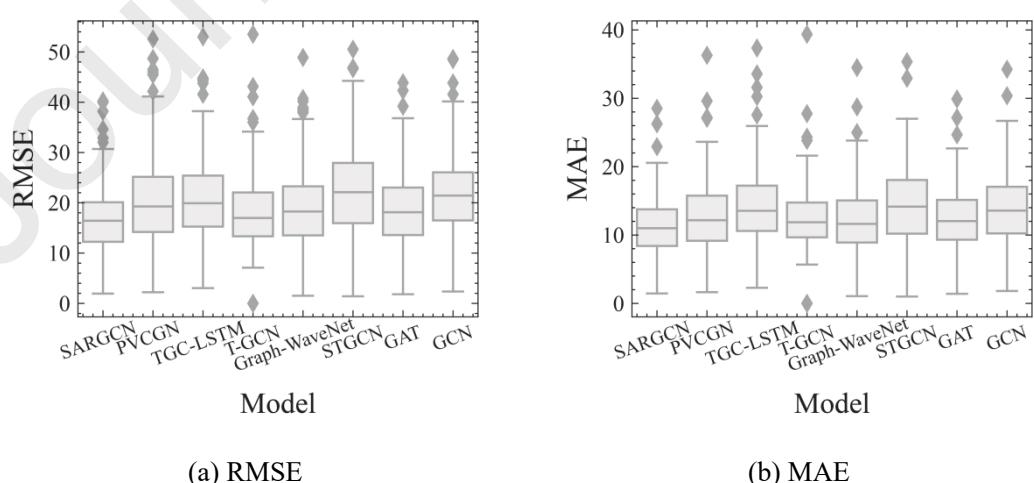


Figure 11 Boxplot of RMSE and MAE for all the GNN-based models on the Shenzhen metro system

1 **5.5 Ablation experiments**

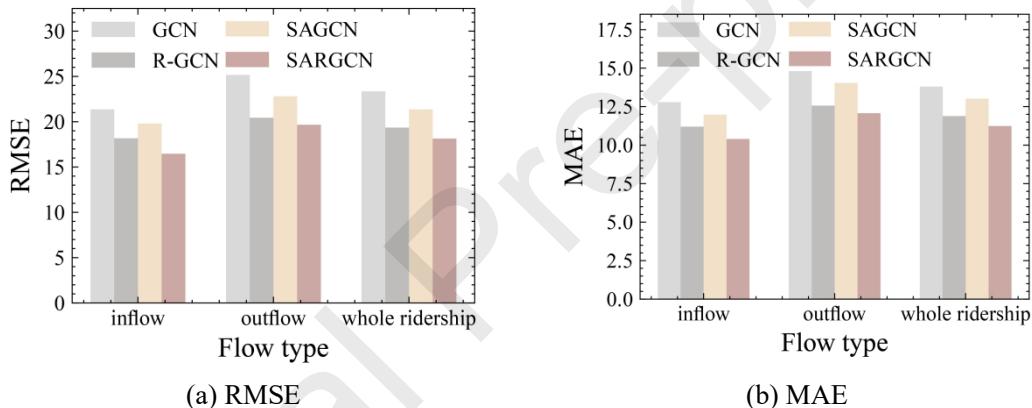
2 According to the model structure, R-GCN (or the knowledge graph) and split-attention  
 3 mechanism are the vital components of the SARGCN model. In this subsection, we further conduct  
 4 an ablation experiment to evaluate the importance of these two components.

5 The prediction performances of GCN, R-GCN, SAGCN (i.e., split-attention graph convolutional  
 6 network), and SARGCN model in the Shenzhen metro system are illustrated in Figure 12, and  
 7 differences among these models are displayed in Table 8. From the prediction results shown in the  
 8 following figures, several conclusions can be summarized.

9 **Table 8 Differences of models in ablation experiment**

Category	Knowledge graph	Split-attention
GCN	✗	✗
R-GCN	✓	✗
SAGCN	✗	✓
SARGCN	✓	✓

10



11 **Figure 12 Ablation experiment results of SARGCN on the Shenzhen metro system**

12 (1) It is evident that R-GCN and SARGCN significantly outperform GCN and SAGCN,  
 13 respectively. For the whole ridership, the RMSE of R-GCN decreases by 17.15% compared with  
 14 GCN on the 1-step prediction task, and SARGCN achieves a 15.10% improvement than SAGCN.  
 15 Therefore, we can conclude that the knowledge graph plays a vital role in metro passenger flow  
 prediction and dramatically improves prediction performance.

16 (2) From the prediction comparison of R-GCN and SARGCN on the whole ridership, we can find  
 17 that RMSE and MAE decrease by 6.23% and 5.44%, respectively. And from the comparison  
 18 between GCN and SAGCN, the improvement reaches 8.51% and 5.67%. Meanwhile, comparing  
 19 SARGCN and R-GCN models on the inflow and outflow, the evaluation metrics express that  
 20 SARGCN can achieve improvement on both inflow and outflow. This is because the split-attention  
 21 mechanism can explore both the temporal dynamics and the dependencies between inflow and  
 22 outflow. Many studies note that the group convolution operation can reduce the number of  
 23 parameters. Although we replace all the convolution operations in the split-attention mechanism  
 24 with R-GCN operation, SARGCN can also achieve parameters reducing by 11.29% (from 829,006  
 25 in R-GCN to 735,372 in SARGCN), thereby leading to a lightweight model.

26 (3) Since the prediction accuracy of SARGCN further outperforms its components, the results of  
 27 the ablation experiment also indicate that the combination of knowledge graph and split-attention

1 mechanism is helpful in improving prediction performance.

2 Furthermore, Figure 13 illustrates the training loss and validation loss during training on the  
 3 Shenzhen metro system. Because we apply the early-stop strategy on these deep learning models to  
 4 avoid overfitting, there is a difference in the epochs when they stop training. Since GCN and  
 5 SAGCN overlook the information on the established knowledge graph, their MSEs are always much  
 6 higher than that of R-GCN and SARGCN. For the models with the split-attention mechanism (i.e.,  
 7 SAGCN and SARGCN), although their convergence speeds are slower than other models, they can  
 8 avoid precocious convergence effectively. Hence, they can search for more appropriate parameters  
 9 to obtain higher accuracies than GCN and R-GCN. According to the principles of SAGCN and  
 10 SARGCN, the main reason for precocious convergence is that there are several parallel models in  
 11 the split-attention mechanism. The prediction performance of SARGCN and SAGCN not only relies  
 12 on the prediction results of each parallel model but also depends on the aggregation of these parallel  
 13 models. Therefore, searching for the appropriate parameters for each model and the aggregators will  
 14 increase the training time, but this increased training time cost can improve prediction performance.

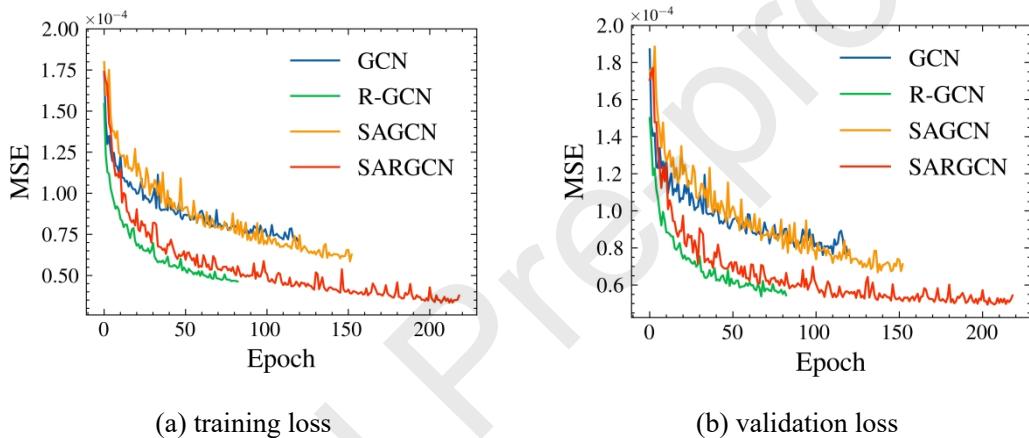


Figure 13 Performance comparison of SARGCN and its corresponding models at different training epochs

## 15 5.6 Graph construction method analysis

16 To validate the effectiveness of the graph construction method, we compare the prediction  
 17 performance of the physical metro network and constructed directed graph of the Shenzhen metro  
 18 system. The comparison results are displayed in Figure 14. Here, both of these graphs are  
 19 transformed to knowledge graphs. To distinguish them, we name these two graphs as the physical  
 20 network and constructed graph, respectively. The results show that the SARGCN based on the  
 21 constructed graph consistently outperforms that on the physical network. Concerning the  
 22 constructed graph, the RMSE and MAE of 1-step prediction are reduced by 5.80% and 6.42%,  
 23 respectively. Moreover, Figure 15(a) and Figure 15(b) show that most metro stations can achieve  
 24 more accurate prediction performance on the constructed graph. Specifically, the percentages of  
 25 stations with a reduced RMSE and MAE are 88.6% and 95.2%, respectively.

26 Besides, we also explore the distributions of the reduced prediction errors in Figure 15(c) and  
 27 Figure 15(d). According to these figures, the reduced prediction errors similarly follow the normal  
 28 distribution, and the average improvement is 1.07 for RMSE and 0.77 for MAE. These  
 29 improvements suggest that the constructed graph has a more powerful capability to capture the  
 30 spatial dependence of the metro system, and combining it with the proposed SARGCN model is an

1 appropriate direction to improve metro passenger flow prediction performance.

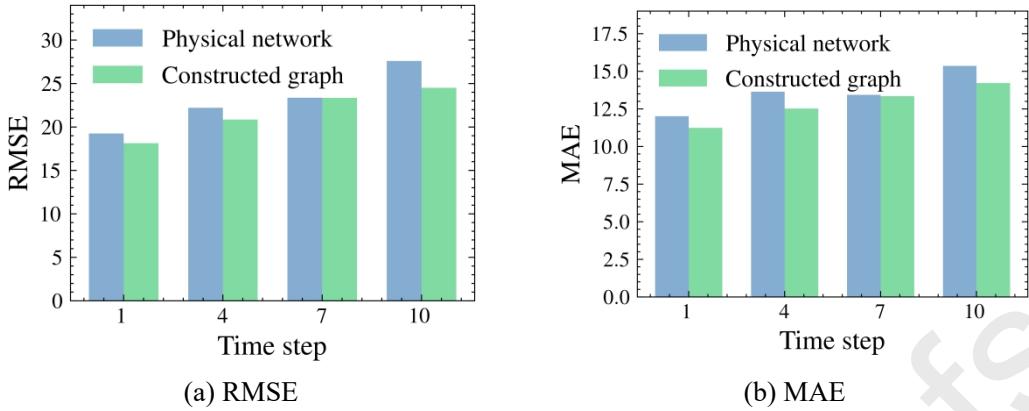
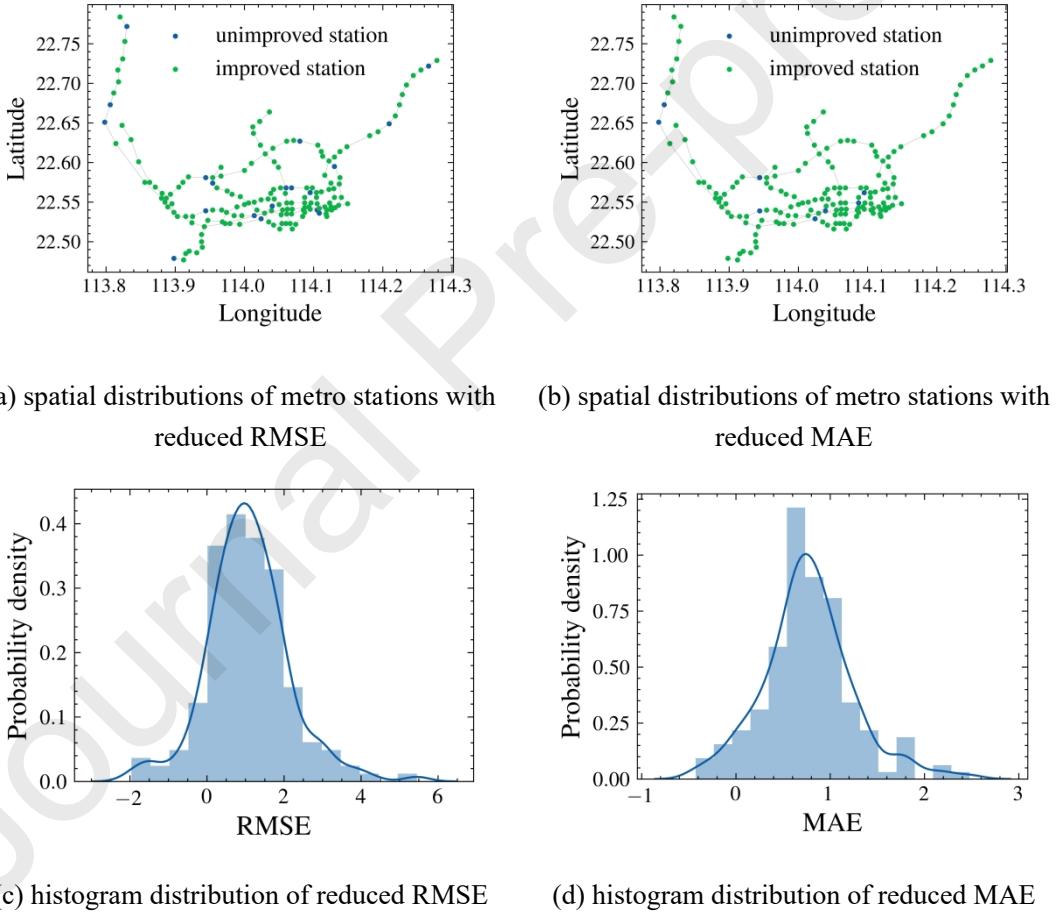


Figure 14 Performance comparison of SARGCN on the constructed graph and physical network in the Shenzhen metro system

2



(a) spatial distributions of metro stations with reduced RMSE (b) spatial distributions of metro stations with reduced MAE

(c) histogram distribution of reduced RMSE (d) histogram distribution of reduced MAE

Figure 15 Distribution of reduced prediction errors by the metro graph construction method in the Shenzhen metro system

3 Moreover, we further analyze the OD passenger flow distributions on these two graphs, and the results are illustrated in Figure 16. In this figure, the OD passenger flows on the self-loop edges are not involved. It is evident that OD passenger flows on the connected edges of the physical network are significantly lower than those of the constructed graph. In other words, there are more frequent passenger flow interactions between the adjacent stations on the constructed graph, while the

1 physical network always ignores these features. Therefore, since the constructed graph can explore  
 2 this dependence from travel behaviors, it can obtain higher prediction accuracy.

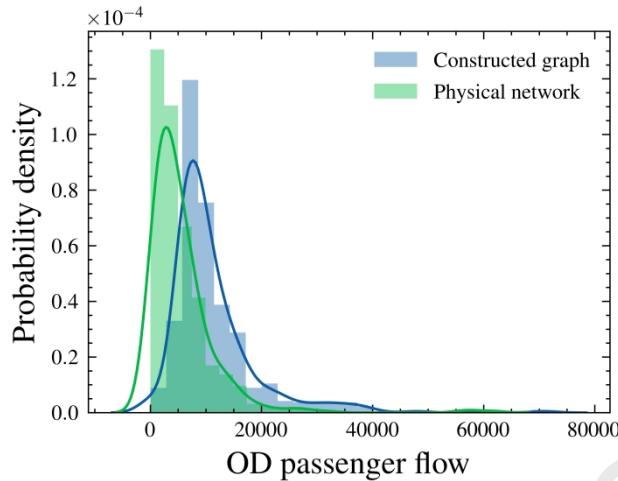


Figure 16 OD passenger flow distribution of the connected edges on the constructed graph and physical network in the Shenzhen metro system

### 3 5.7 Knowledge graph analysis

4 The prediction performance comparisons in Section 5.5 demonstrate that the established  
 5 knowledge graph positively impacts prediction accuracies. In this subsection, we further explore the  
 6 properties of the knowledge graph.

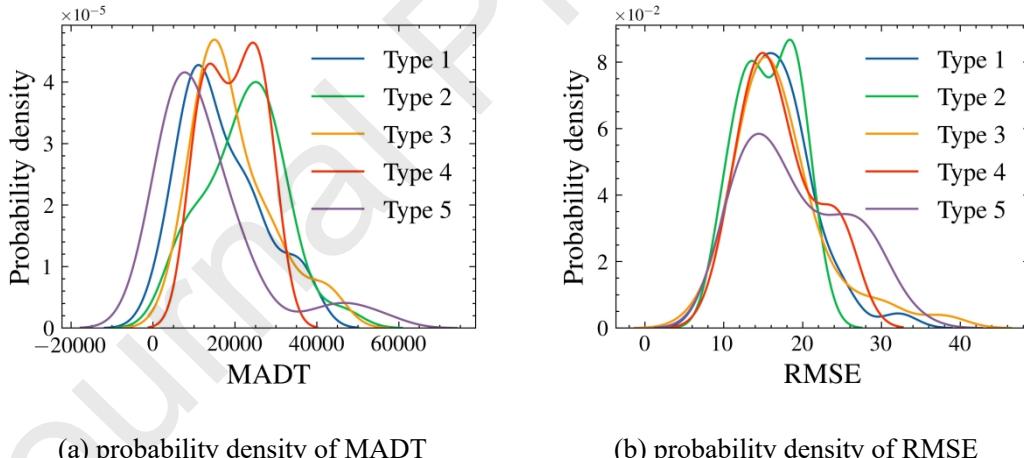


Figure 17 Traffic features distributions between different types of stations in the Shenzhen metro system

7 In the established knowledge graph, the proportion of metro stations with different semantic types  
 8 is 24.7%: 15.7%: 22.9%: 10.8%: 25.9%. Among all the types, stations with type 1 (i.e., resident  
 9 area) account for the largest proportion. Moreover, Figure 17(a) and Figure 17(b) illustrate the  
 10 probability density distribution of monthly average day traffic (MADT) and RMSE under different  
 11 semantic types. According to the MADT distribution, each type has its unique characteristics, and  
 12 these differences can be effectively distinguished by the knowledge graph construction method.  
 13 Meanwhile, an interesting finding is obtained from the probability density distribution of MADT  
 14 and RMSE. For instance, the MADT distribution of type 5 is always lower than that of type 2.  
 15 However, as the RMSE distribution comparison shows, the probability density of type 5 is much

1 higher than type 2 when RMSE is higher than 20. The reason may be that type 5 includes many  
 2 transfer nodes with other modes of transportation (e.g., buses, railways, and airplanes). Hence,  
 3 passenger flows at these stations mainly originate from other transportation modes. The imbalanced  
 4 schedules of other transportation modes easily produce randomness and instabilities in metro  
 5 passenger flows. Therefore, it brings significant challenges for accurate prediction, leading to higher  
 6 prediction errors. This finding reveals that the knowledge graph can capture and distinguish the  
 7 travel patterns of each station type to promote spatial correlation mining.

8 **6. Conclusion**

9 This study proposes a deep learning framework named split-attention relational graph  
 10 convolutional network (SARGCN) to address the network-scale metro passenger flow prediction.  
 11 Unlike previous studies, which directly apply the physical metro network for GNNs, we develop a  
 12 metro knowledge graph construction method to adapt the travel behavior. Specifically, the historical  
 13 OD matrix is extracted and employed as the similarity measure to construct the metro topological  
 14 graph. Then, we utilize the land-use features to represent the semantic types of each station, aiming  
 15 to establish a knowledge graph based on the constructed directed graph. To further explore the  
 16 spatiotemporal dependencies on the established knowledge graph, we propose the SARGCN model,  
 17 by integrating the R-GCN, split-attention mechanism, and LSTM. Validated on the Shenzhen and  
 18 Hangzhou metro system, SARGCN expresses superiority compared to widely-used baselines and  
 19 state-of-the-art methods.

20 However, this study still has several limitations. For instance, various payment methods, such as  
 21 smart cards and mobile payments, have been developed for metro systems in recent years. However,  
 22 due to the barriers in research data collection, this study only extracts the smart card data for  
 23 passenger flow analysis and prediction. Since passenger travel behavior may differ by payment  
 24 method, fully considering these differences might enhance spatiotemporal correlation analysis.  
 25 Moreover, many studies demonstrate that external information, such as weather and special events  
 26 (Xue et al., 2022), also impacts the metro passenger flow, which is not involved in this study.

27 According to the limitations and challenges of this study, the following suggestions might be  
 28 interesting directions for future work.

29 (1) Metro is a critical component in the urban transit system, and its passengers always source  
 30 from other transportation modes, e.g., buses, bike-sharing, etc. So, introducing the real-time  
 31 passenger distributions of other transportation modes may improve prediction performance.

32 (2) In addition to predicting the inflow and outflow, OD passenger flow prediction (Dai et al.,  
 33 2018; Hussain et al., 2021; Zhang et al., 2021) is also a hot topic in this field. From the essence of  
 34 these two passenger flows, the former denotes the number of passengers entering and exiting the  
 35 metro system, and the latter reflects the passenger flow direction and evolution process within this  
 36 system. Future works can further explore the dependence between these two flows and integrate  
 37 these two tasks to improve prediction performance.

38 (3) An increasing number of researchers have paid attention to inductive learning tasks in traffic  
 39 prediction (Wu et al., 2020). Graph neural networks with inductive learning ability can be applied  
 40 to different topology networks and achieve acceptable performance. Since metros are rapidly  
 41 constructed and developed, a robust model with strong generalization to different topological graphs  
 42 is needed. Thus, inductive learning has excellent potential in metro passenger flow prediction.

1 **Appendix**

2 The important abbreviations used in this study is summarized as follows.

3 Table 9 The important abbreviations used in this paper

Abbreviations	Description
GCN	Graph convolutional network.
GNN	Graph neural network.
LSTM	Long short-term memory network.
MADT	Monthly average day traffic of passenger flow.
MAE	Mean absolute error, mathematically expressed by Equation 24.
MAPE@10	Mean absolute percentage error (MAPE) on metro stations with the top 10% largest passenger flow.
OD matrix	Origin-destination (OD) matrix.
POI	Point of interest data, which represents the land-use characteristics in the urban area.
R-GCN	Relational graph convolutional network.
RMSE	Root mean square error, mathematically expressed by Equation 23.
SAGCN	Split-attention graph convolutional network, which use the GCN layer to replace the R-GCN layer in SARGCN.
SARGCN	Split-attention relational graph convolutional network proposed by this study.

4 **Acknowledgments**5 This research is funded by the National Natural Science Foundation of China (No. 52172310),  
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5

6 **Highlight**

7

- 8 ● This paper models the metro system as knowledge graph for passenger flow  
9 prediction.
- 10 ● It combines traffic patterns and land-use features for knowledge graph  
11 construction.
- 12 ● It proposes a SARGCN model for spatiotemporal prediction on metro  
13 knowledge graphs.
- 14 ● It uses an attention mechanism to learn the correlation between inflow and  
15 outflow.
- 16 ● Validated on two metro datasets, it outperforms numerous advanced baselines.

17

18 **Jie Zeng:** Conceptualization, Methodology, Software, Writing-Original draft  
19 preparation. **Jinjun Tang:** Conceptualization, Writing- Reviewing and Editing,  
20 Visualization.

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